

ANR ESRR

Kick-off meeting 2017, March

Stellar rotation: Roche-von Zeipel model

Roche potential (point-like gravitational + centrifugal potentials):

$$\Psi = -\frac{GM}{R(\theta)} - \frac{\Omega^2 R^2(\theta) \sin^2 \theta}{2} = -\frac{GM}{R_p} = -\frac{GM}{R_{eq}} - \frac{(\Omega R_{eq})^2}{2}$$

$$\vec{g}_{\text{eff}} = -\vec{\nabla}\Psi = \vec{g} + \vec{a}_{\text{cent}}$$

$$\frac{\vec{\nabla}P}{\rho} = \vec{g}_{\text{eff}} = -\vec{\nabla}\Psi \quad (\text{hydrostatic equilibrium})$$

von Zeipel-like gravity darkening:

$$\vec{F} = -\chi \frac{dT}{d\Psi} \vec{\nabla}\Psi = \chi \frac{dT}{d\Psi} \vec{g}_{\text{eff}} \equiv -C \vec{g}_{\text{eff}}$$

$$F = \sigma T_{\text{eff}}^4 = C g_{\text{eff}}$$

von Zeipel (1924)



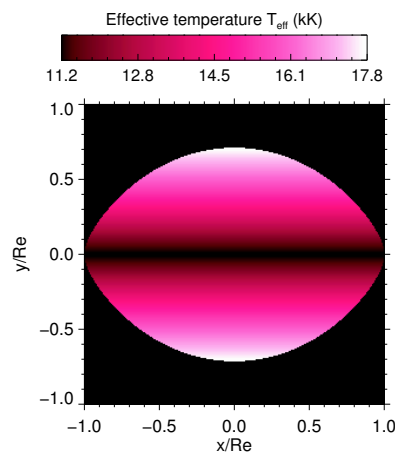
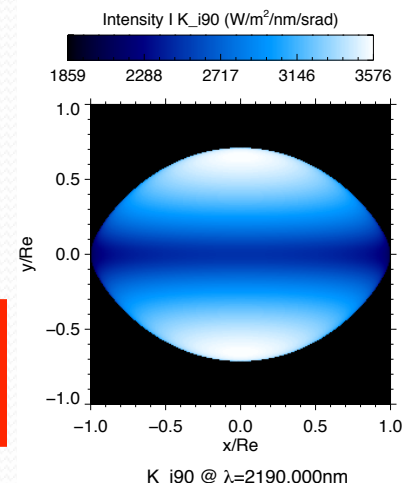
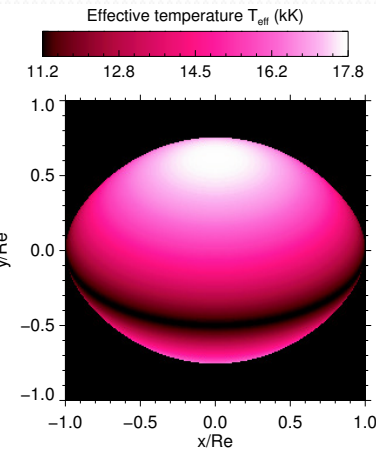
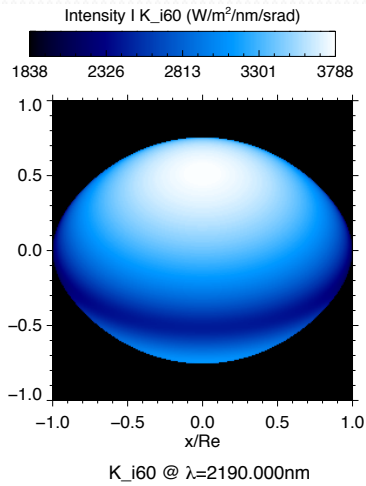
generalize

$$F = \sigma T_{\text{eff}}^4 = C_{\beta} g_{\text{eff}}^{4\beta}$$

β parameter

$$T_{\text{eff}} = \left(\frac{C_{\beta}}{\sigma}\right)^{0.25} g_{\text{eff}}^{\beta}$$

$$T_{\text{eff}} = \left(\frac{C}{\sigma}\right)^{0.25} g_{\text{eff}}^{0.25}$$



Apparent intensity distribution dependent on inclination. T_{eff} variable over photosphere.

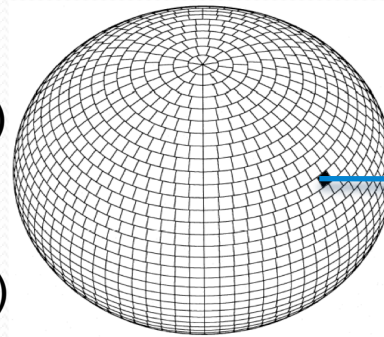
CHARRON

Code for High Angular Resolution of Rotating Objects in Nature

Domiciano de Souza et al. 2002, 2012

$M, v_{\text{eq}}, R_{\text{eq}},$
 $\langle T \rangle$ (ou L),
 i, d, β

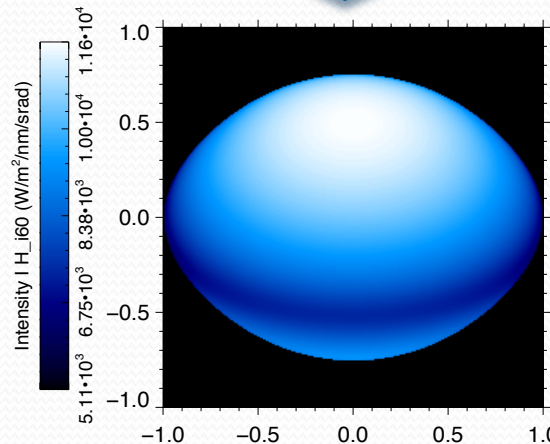
Surface potential Ψ
(e.g. Roche potential)
 $\rightarrow g_{\text{eff}} = |-\text{grad } \Psi|$
 $\rightarrow T_{\text{eff}} = C g_{\text{eff}}^\beta;$
 $C = C(M, \langle T \rangle, v_{\text{eq}})$



At each surface
grid element:

$\theta, \phi, \mu, T_{\text{eff}}, g_{\text{eff}}$
 $v_{\text{proj}}, dS_{\text{proj}}$

Specific intensities
 $I_\lambda = I_\lambda(\mu, T_{\text{eff}}, g_{\text{eff}})$
from stellar
atmosphere models
(e.g. Kurucz or
TLUSTY + Synspec)

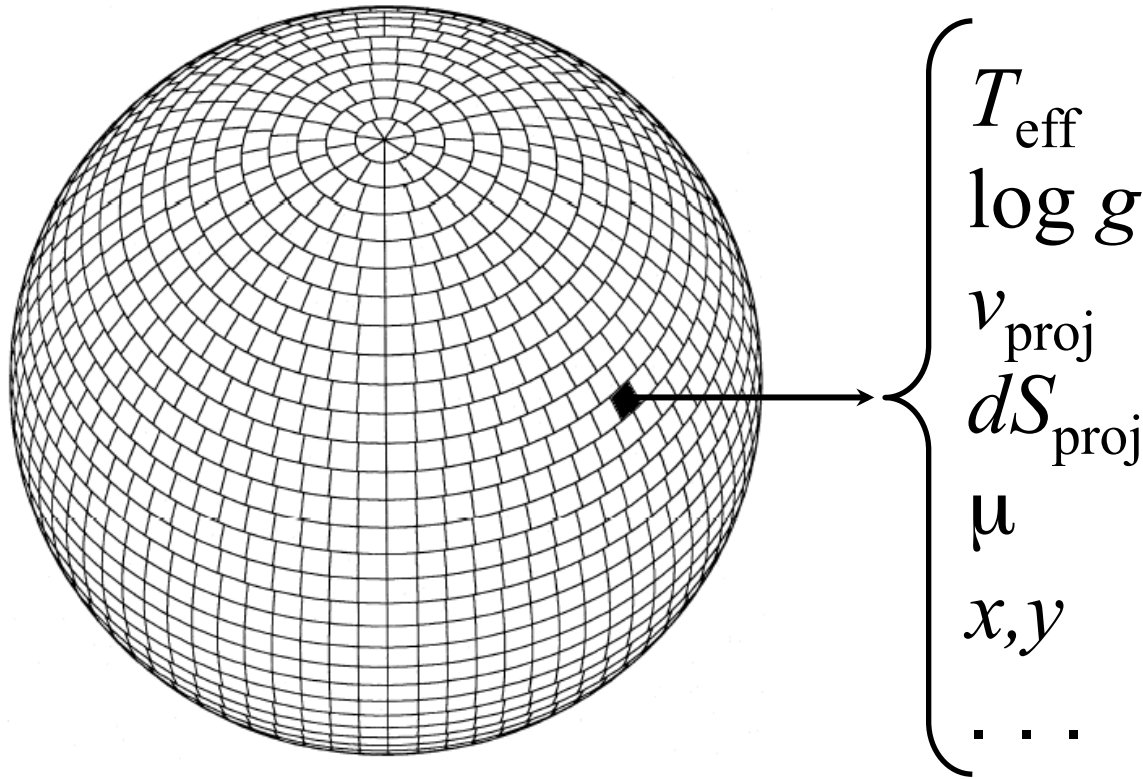


Intensity maps $I_\lambda(\theta, \phi)$
of stellar photosphere

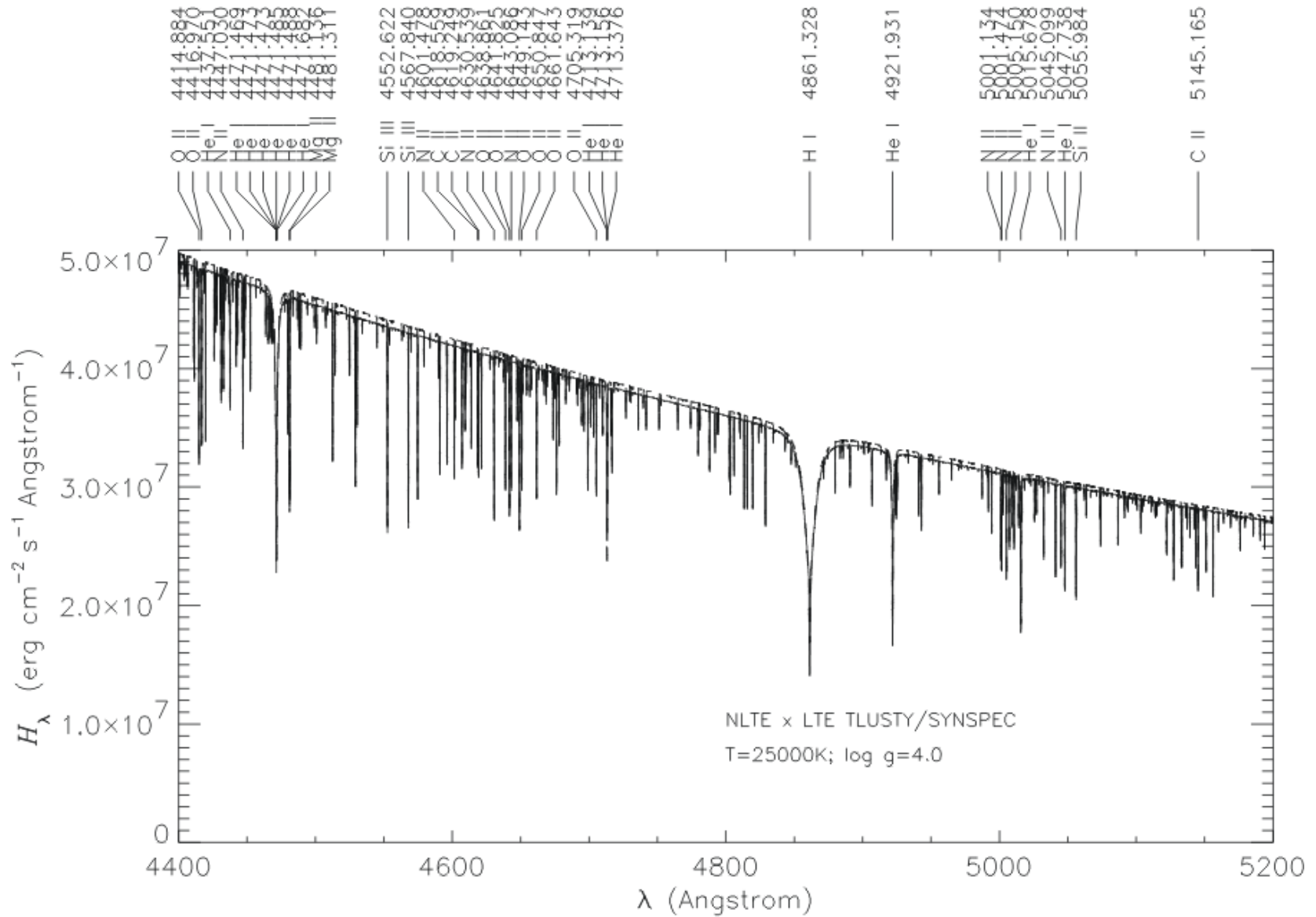
(computation time ~ 10 -30s)

CHARRON: ancien m tier;
spcialiste du bois, ma tre de
tout ce qui tourne et roule.

Paramètres physiques et grille numérique



Synthèse de profils spectraux



Questions

Comment associer des modèles d'atmosphère plan-parallèles (e.g. Kurucz, TLUSTY) et des spectres (e.g. SYSNPEC, PHOENIX, MARCS) à ESTER ?

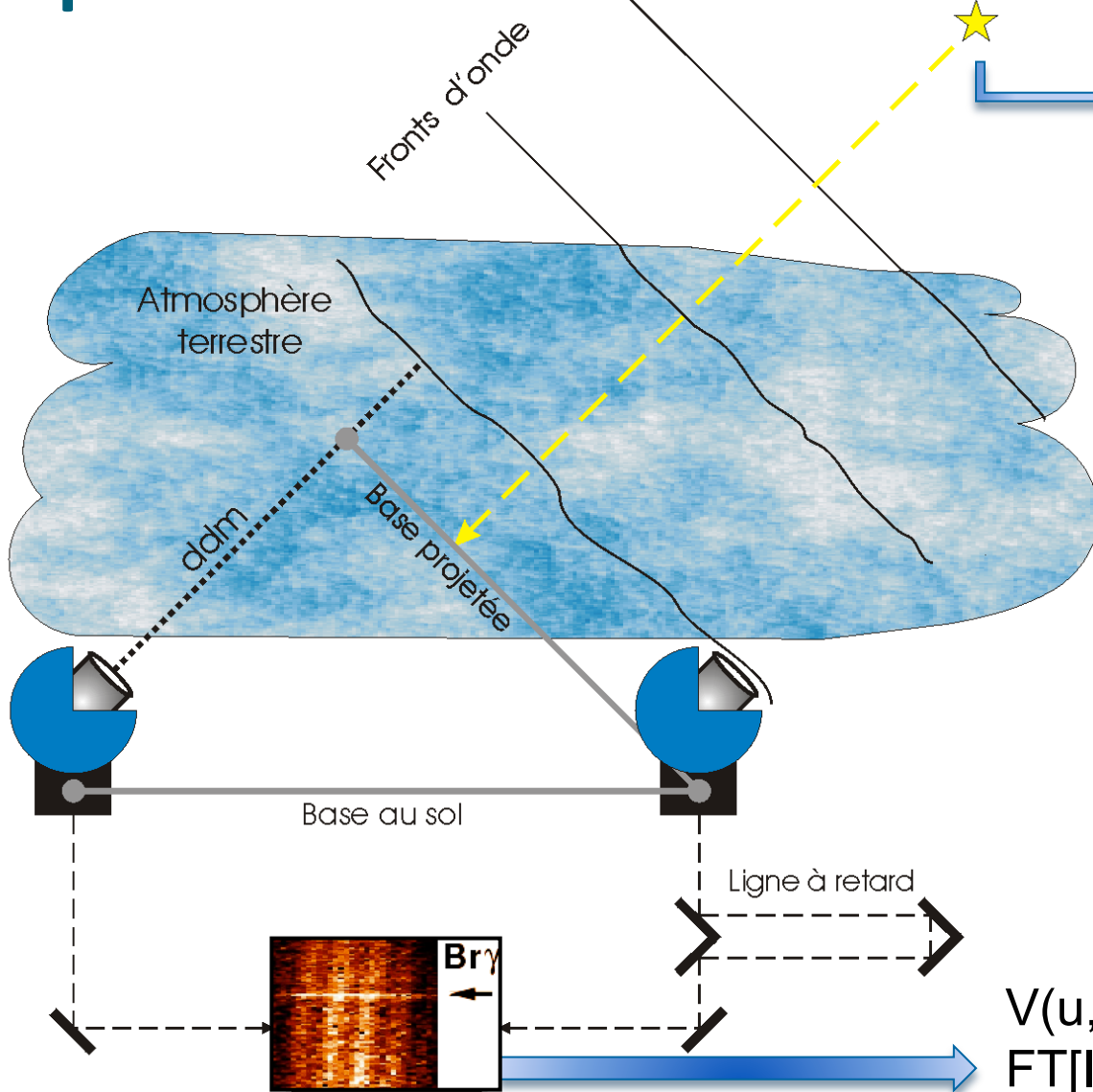
Quelle « profondeur » prendre dans les modèles ESTER pour associer un spectre synthétique ?

Ce problème ne se pose pas dans un modèle de Roche, et plusieurs personnes l'ont fait (e.g. Domiciano de Souza et al. Papers). Il y a aussi un papier de Kurucz de 2014 qui traite cette question.

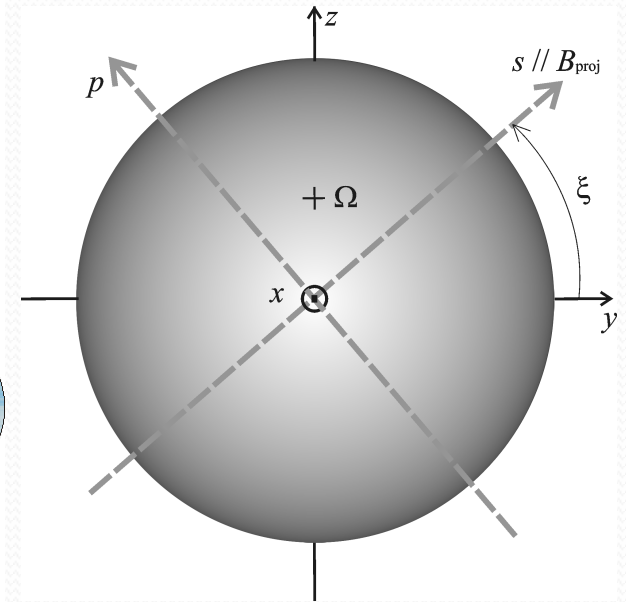
Observations interférométriques d'étoiles en rotation rapide



Spectro-interferometry



Intensity map $I(y,z,\lambda)$



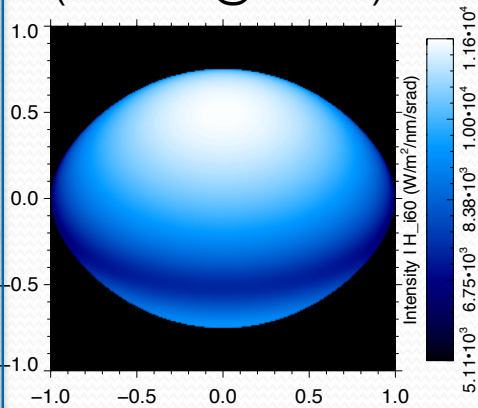
Interference fringes \rightarrow
 complex visibility V
 (Fourier transform of I):

$$V(u,v,\lambda) = \frac{FT[I(y,z,\lambda)](u,v)}{FT[I(y,z,\lambda)](0,0)}$$

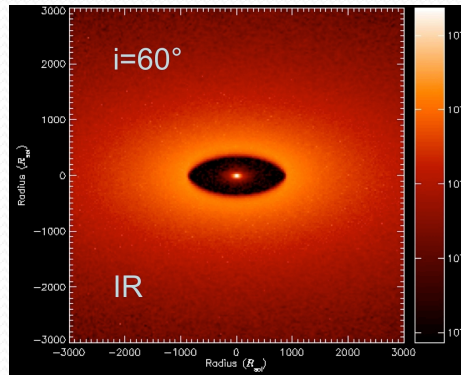
Spectro-interferometry

Intensity maps from physical models

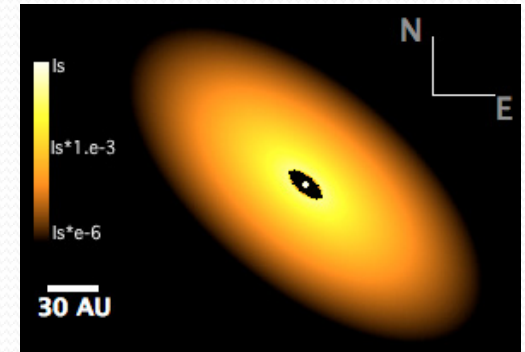
CHARRON
(~10-30s @ 1 CPU)



HDUST
(~5-10h @ 100 CPU)



FRACS
(~1-10s @ 1 CPU)



Model fitting

Integrate or
Fourier
transform

Spectro-interferometric observables: fluxes (spectra), SED, photometry, absolute and differential visibilities (amplitudes and phases), closure phases.

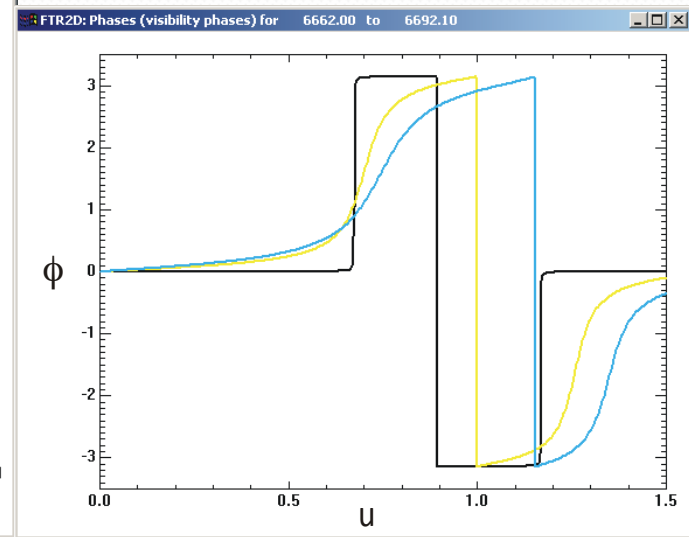
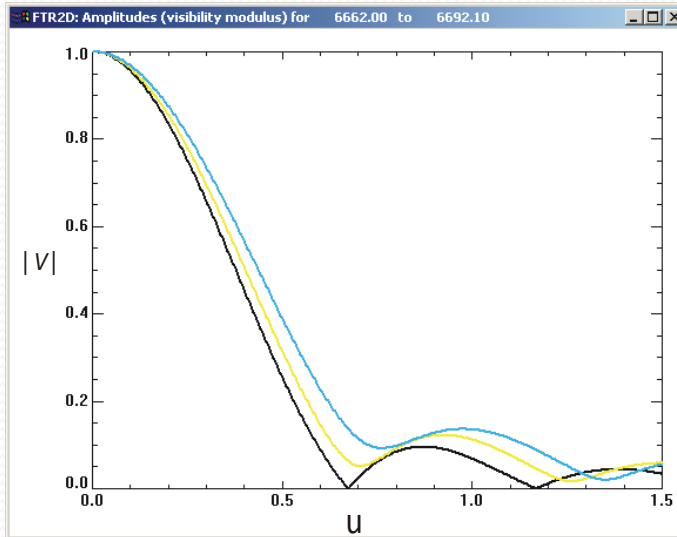
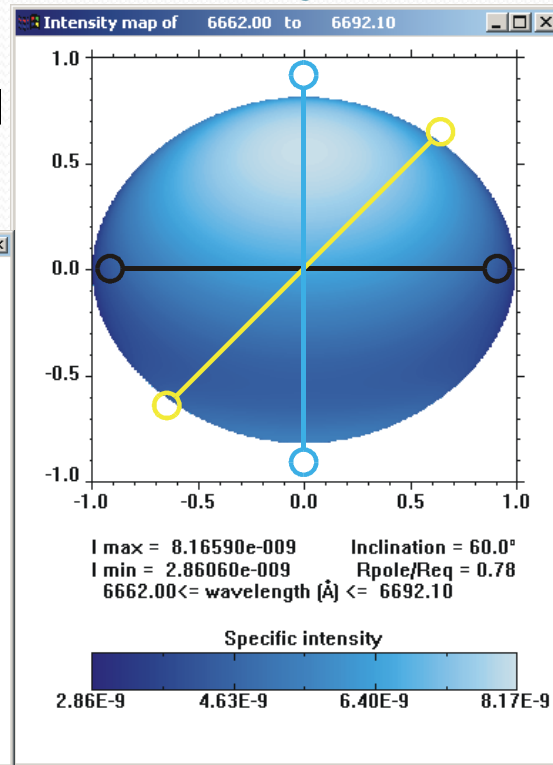
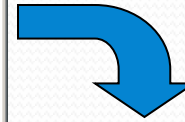
Spectro-interferometry

Intensity map

Complex visibility
amplitude $|V|$
(fringe contrast)



Complex visibility
phase ϕ
(fringe position)



Closure phase

$$\begin{aligned} \Phi_{ijk} &= \phi_{\text{obs}}(u_{ij}, v_{ij}) + \phi_{\text{obs}}(u_{jk}, v_{jk}) + \phi_{\text{obs}}(u_{ki}, v_{ki}) \\ &= \phi(u_{ij}, v_{ij}) + \phi(u_{jk}, v_{jk}) + \phi(u_{ki}, v_{ki}) \end{aligned}$$

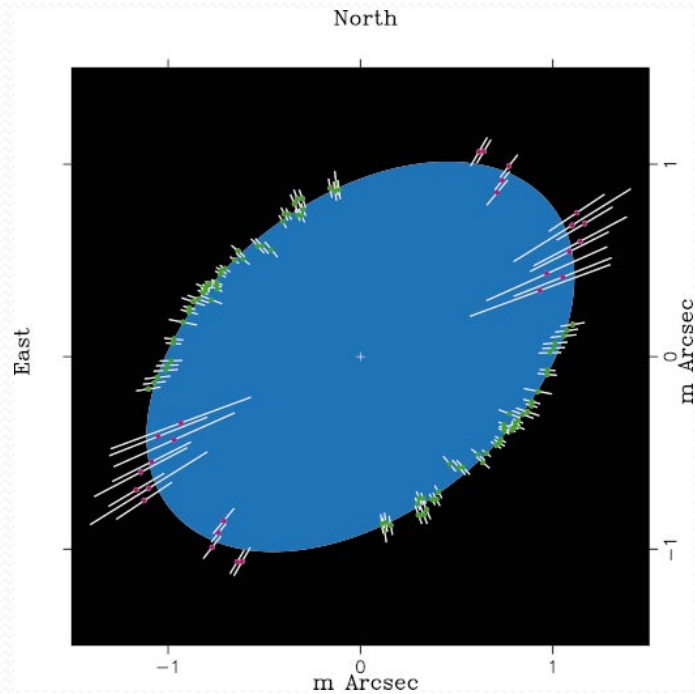
Differential phase

$$\phi_{\text{diff}} = \phi - \left(a + \frac{b}{\lambda} \right)$$

ϕ not directly
accessible



Achernar: ideal fast-rotator target for HRA



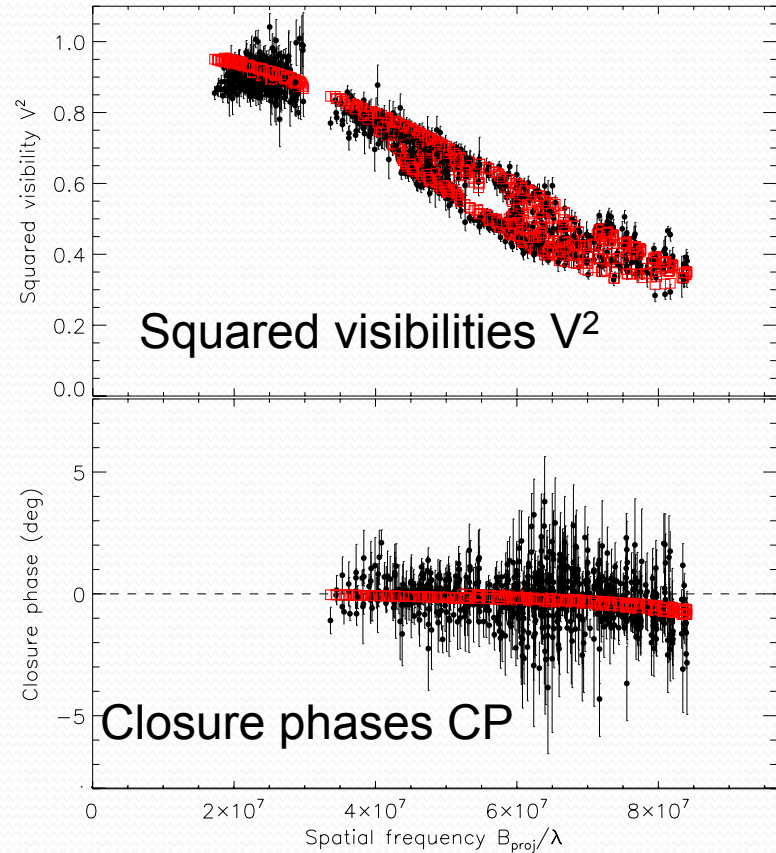
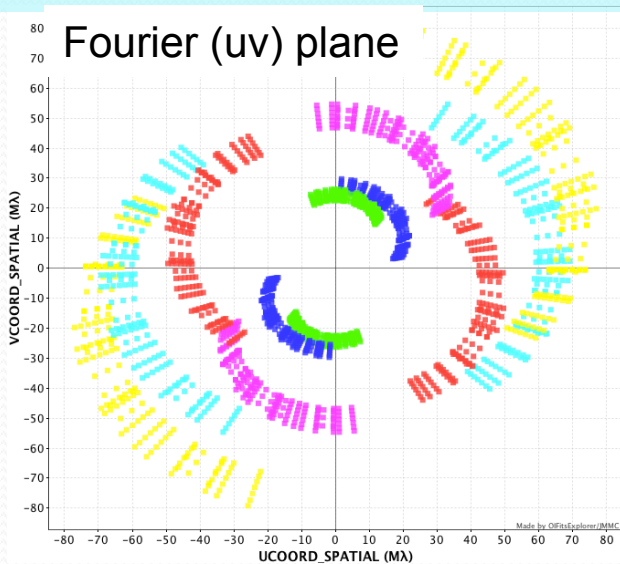
Domiciano de Souza, Kervella et al. 2003
(VLT/VINCI Sep-Nov/2002 data)
Press release ESO

Some information on Achernar:

- ✧ B3-6Vpe star
- ✧ $V=0.5$ (brightest Be star)
- ✧ $M \sim 6 M_{\text{sun}}$
- ✧ $d=42.7$ pc (closest Be star)
- ✧ Mean $T_{\text{eff}} \sim 15000\text{K}$
- ✧ $v \sin i \sim 260$ km/s (wide range of values in the literature)
- ✧ Strong rotation flattening (beyond Roche limit)

Achernar: VLTI/PIONIER observations

- Simultaneous observations 4 AT
- V^2 and CP
- H band (3 & 7 spectral channels)
- Baselines from ~ 30 to 120 m
- Observations in 8-9/2011 and 9/2012



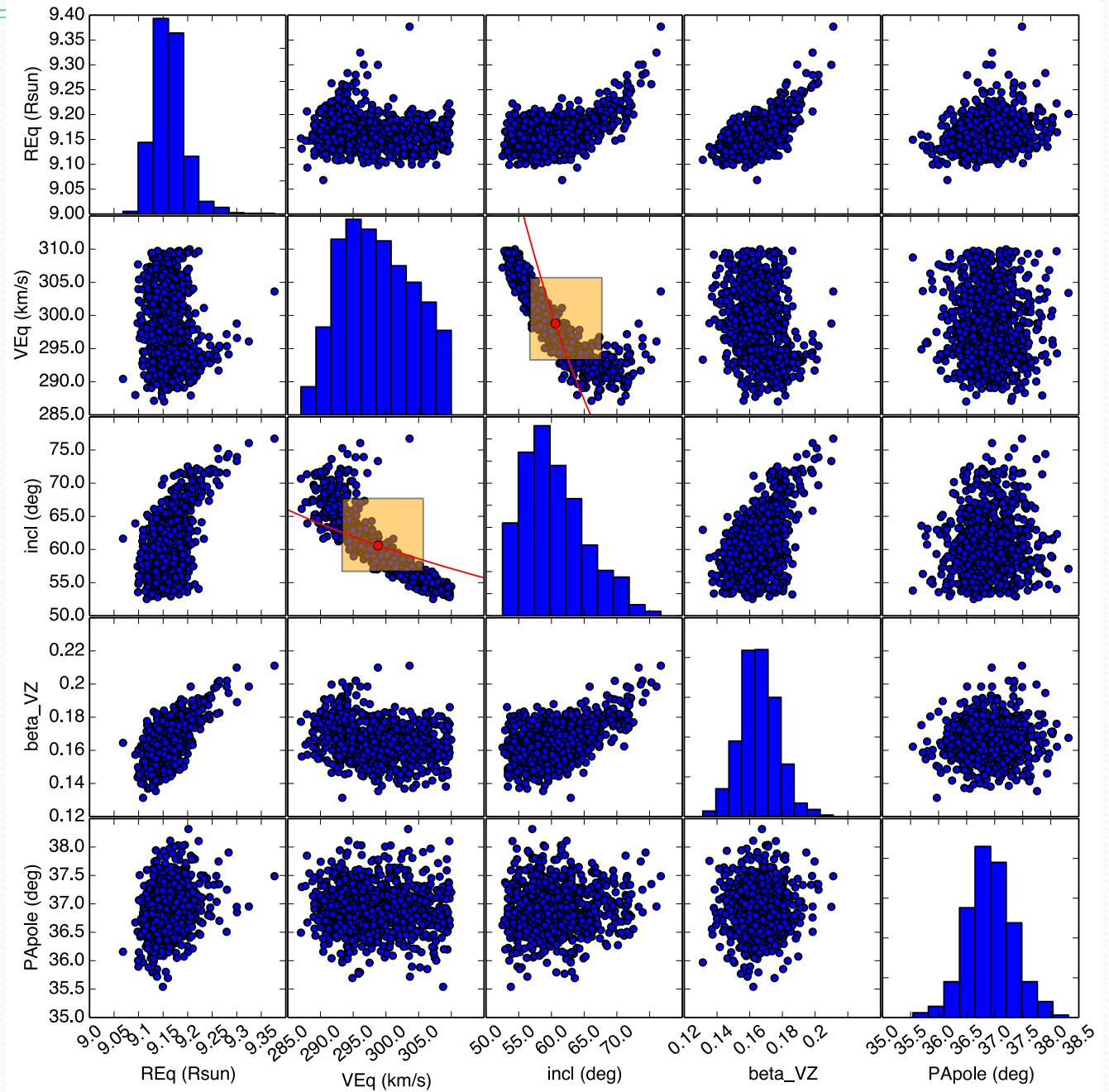
Study Achernar as a fast-rotator but...keep in mind that this star is also a:

- ✧ Be star: episodic emission phases from disque (variations at several time scales)
- ✧ Binary (orbital period ~ 7 years) \rightarrow out of FOV from PIONIER

Domiciano de Souza
et al. 2014, A&A

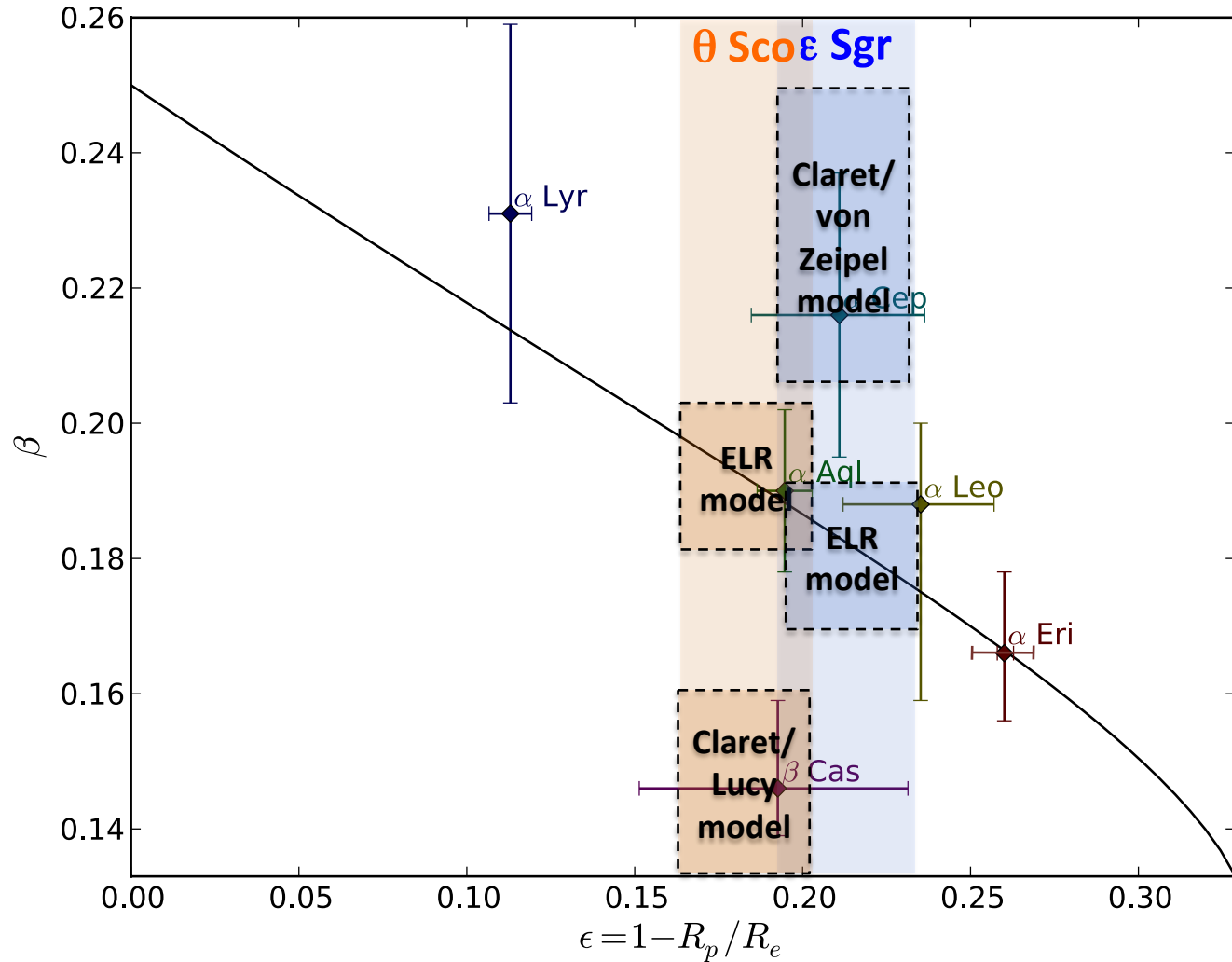
Achernar parameters

MCMC fitting

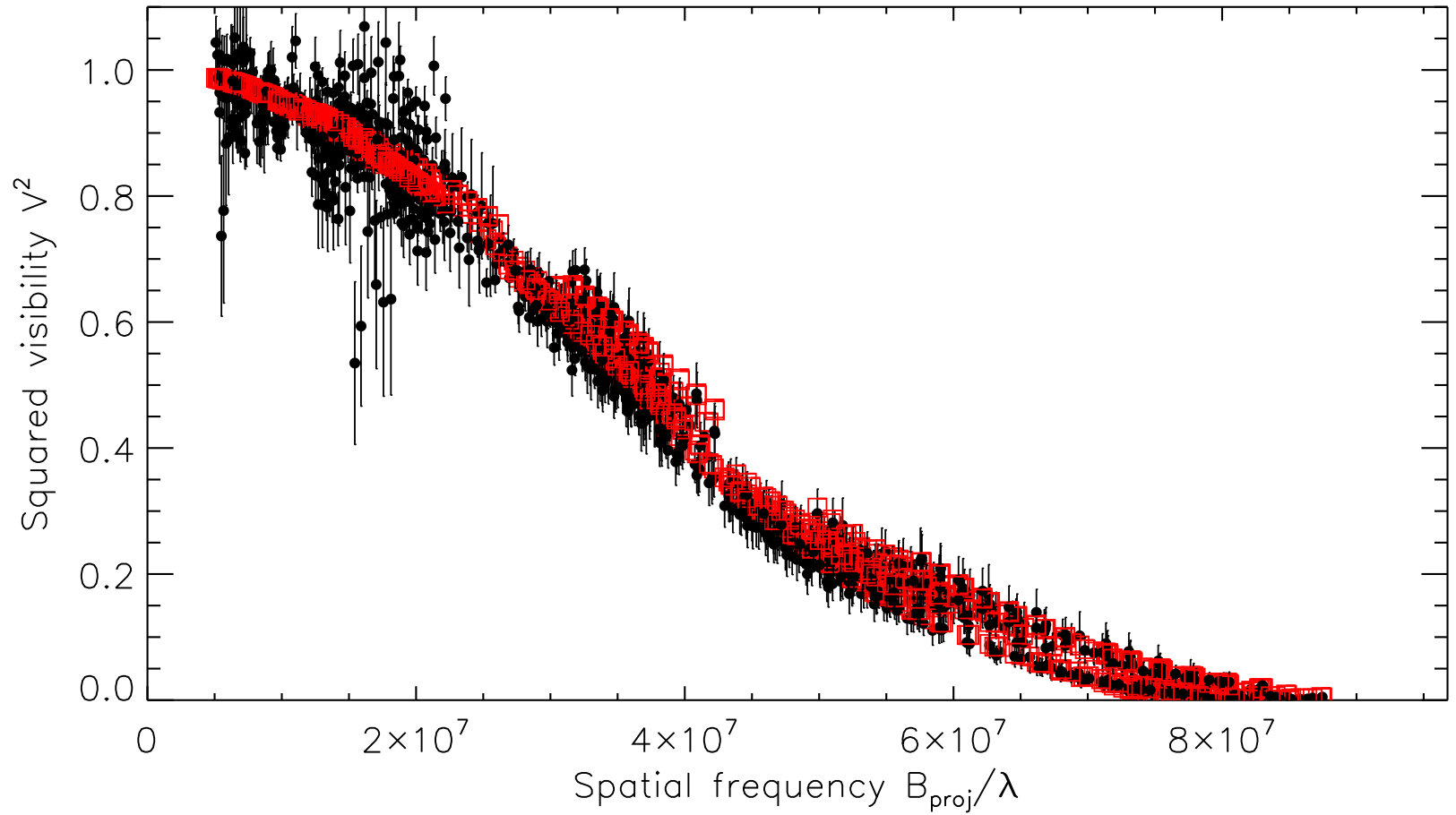


ESO P97

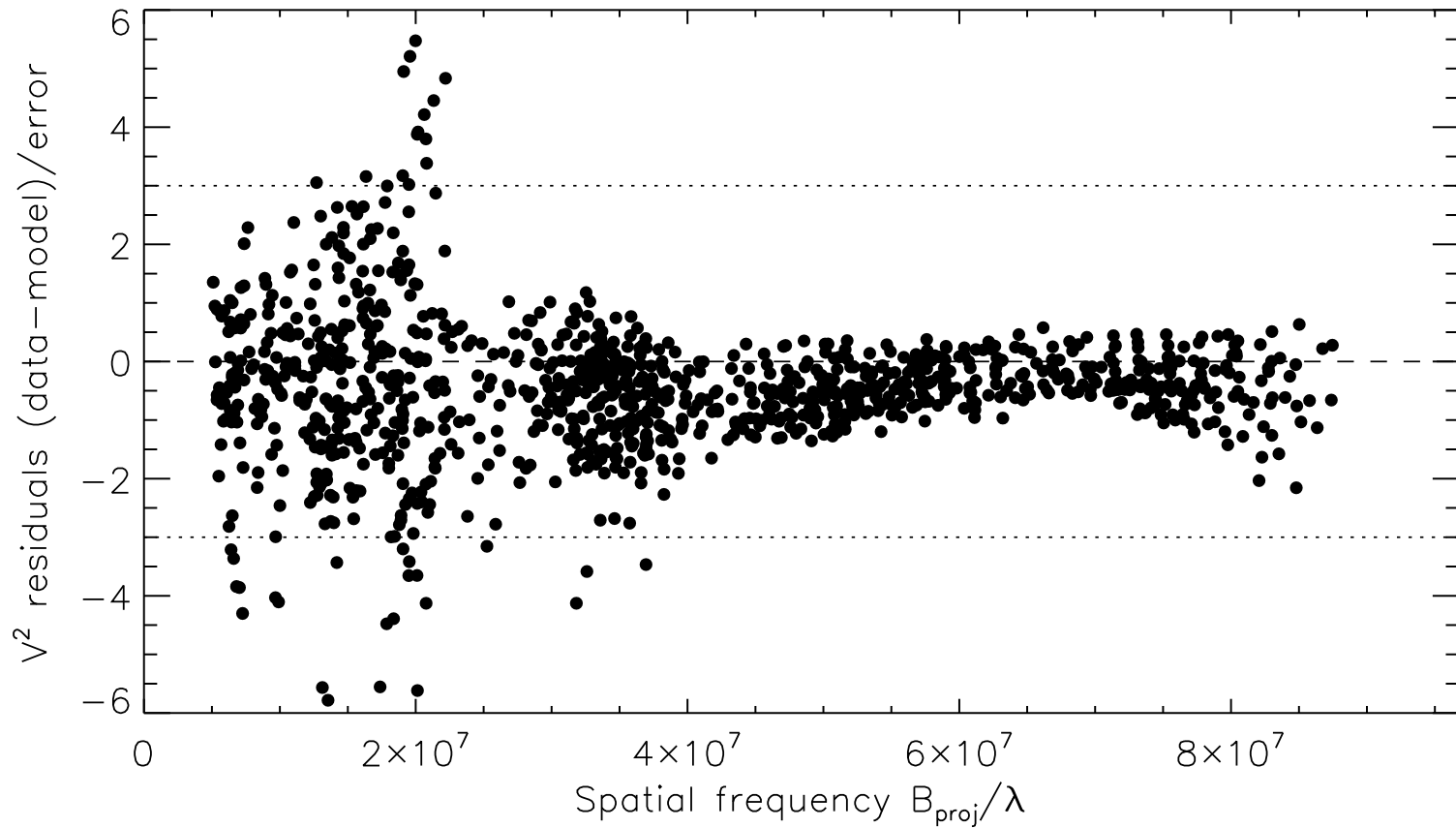
Stellar gravity darkening put into test



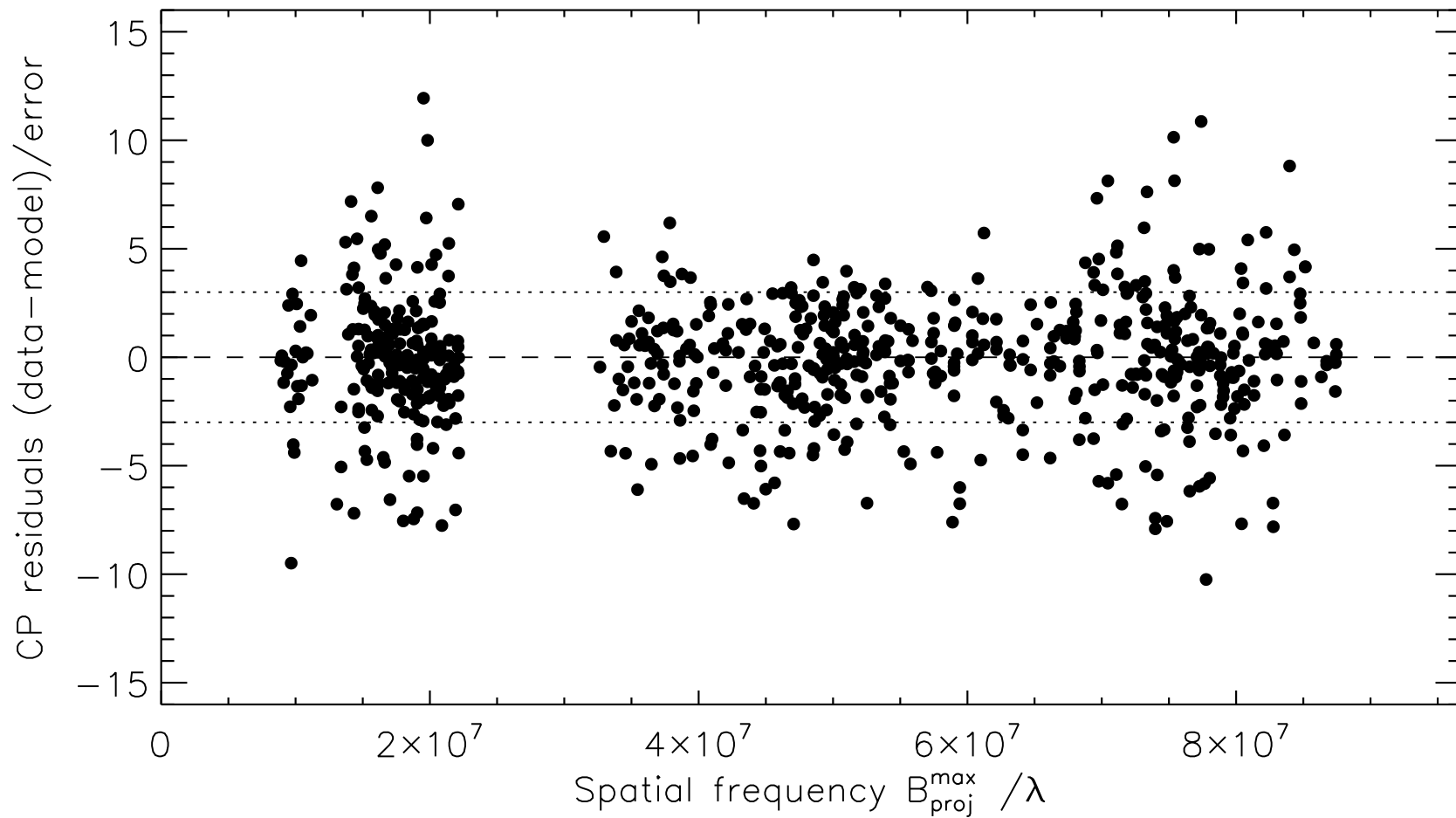
theta Sco (F1III)



theta Sco (F1III)



theta Sco (F1III)



theta Sco (F1III)

Distance d (pc)	= 91.158	Polar axis inclination i (deg)	= 58.721
Equatorial Radius Req (Rsun)	= 29.996	Equatorial angular diameter (mas)	= 3.0618
Polar Radius Rpol (Rsun)	= 25.436	Polar angular diameter (mas)	= 2.5964
Req/Rpol	= 1.1793	Rpol/Req	= 0.84799
Equal Area Radius (Rsun)	= 28.28	Equal Volume Radius (Rsun)	= 28.202
Equatorial Temperature Teq (K)	= 6231.8	log Equatorial Gravity log geq (cgs dex)	= 2.0437
Polar Temperature Tpol (K)	= 7681.4	log Polar Gravity log gpol (cgs dex)	= 2.3798
Mean Temperature Tmean (K)	= 6836.7	Stellar Mass M (Msun)	= 5.66
Stellar Luminosity L (Lsun)	= 1568.1	log(L/Lsun)	= 3.1954
Mean bolom. flux Fbol=L/(4PI*d^2) (W/m^2)	= 6.0657E-09	Mean mag_bol=-2.5log(Fbol/2.53E-8)	= 1.5506
Equatorial rotation velocity Veq (km/s)	= 113.59	Equatorial rotation period Peq (h)	= 320.8
Ve sin i (km/s)	= 97.084	Equatorial angular vel. Omega_eq (cyc/day)	= 0.074822
Ve/Vcrit (eta=1)	= 0.59876	Omega_eq/Omega_crit (eta=1)	= 0.59876
Ve/Vcrit (Roche)	= 0.67529	Omega_eq/Omega_crit (Roche)	= 0.85897
eta = Omega_eq^2 Req^3/GM	= 0.35851	tau = E_cinet/E_pot	= 0.0071777
von Zeipel coefficient beta	= 0.27029		